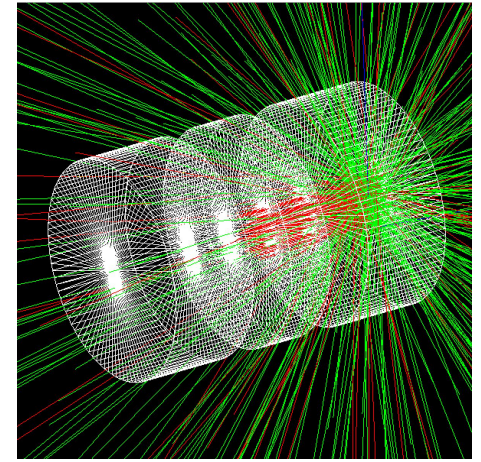


Muon Catalyzed Fusion (MCF)

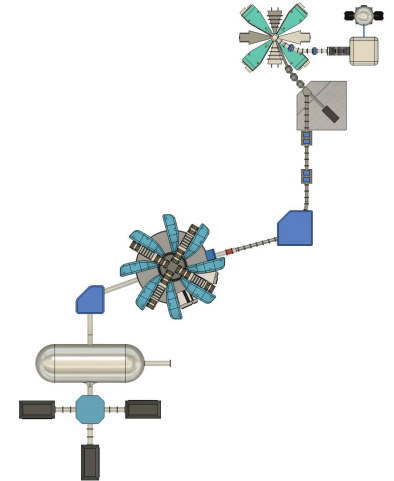


Himani Mishra and Thomas Rimer
04.24.2026

1. MCF Reaction Dynamics and Geant4 Simulation - Himani

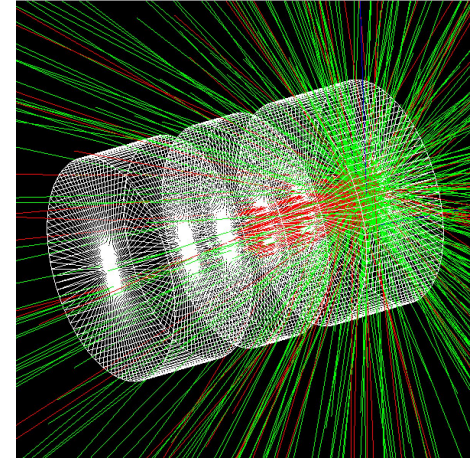


2. Designing a Muon Source in CAD - Thomas



1. MCF Reaction Dynamics and Geant4 Simulations - Himani

- a. MCF Reaction
- b. Geant4
- c. Simulation Geometry
- d. Reaction Rates & Constants
- e. Experiments - Initial Energy, Temperature, Pressure, T:D Ratio
- f. Reaction Dynamics Takeaways

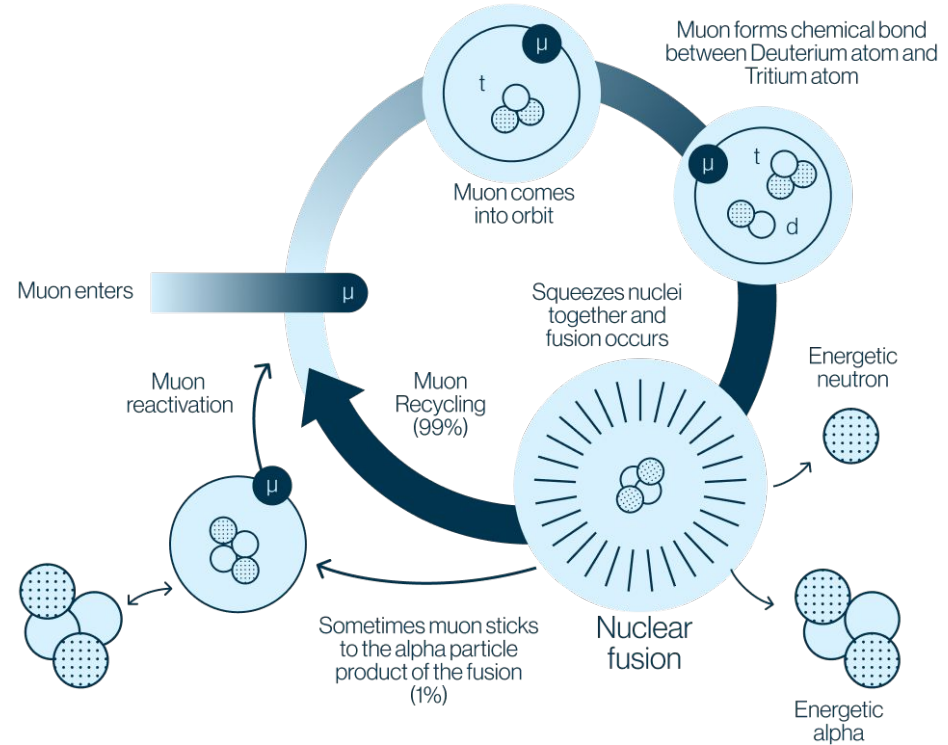


The Reaction

- Muon: a negatively charged particle, ~207 times mass of electron
→ **Catalyzes the reaction!**
- Reaction:
 - Alpha Sticking: $dt\mu \rightarrow \alpha\mu + n + 14.1 \text{ MeV}$
 - No Alpha Sticking: $dt\mu \rightarrow \alpha + \mu + n + 14.1 \text{ MeV}$

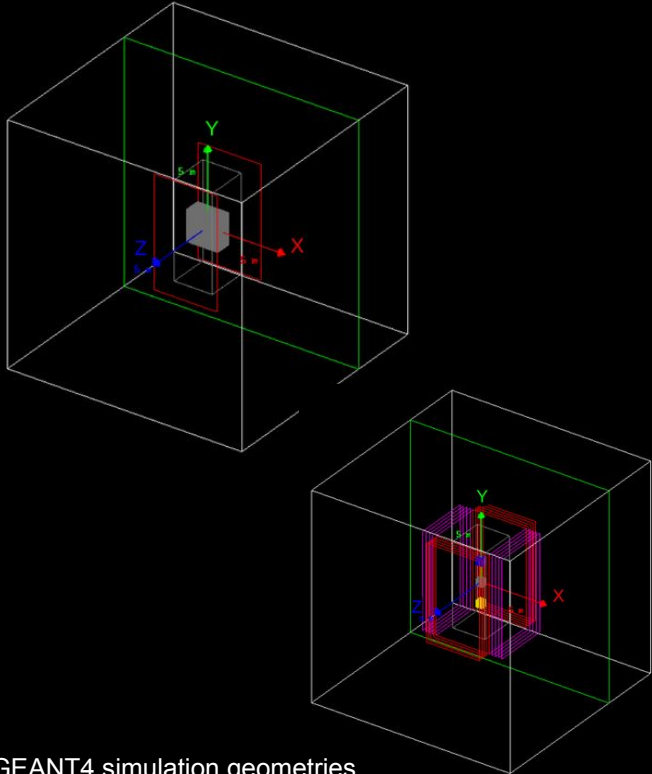
→ **Advantage: low temperature**
1300 K \ll 100 million K

→ **Challenge: Alpha sticking +**
Muon generation



<https://www.acceleron.energy/>

Geant4

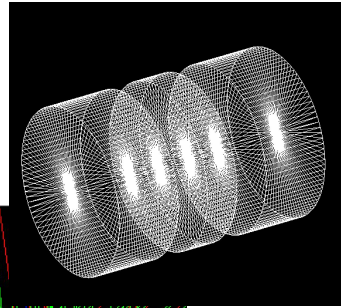
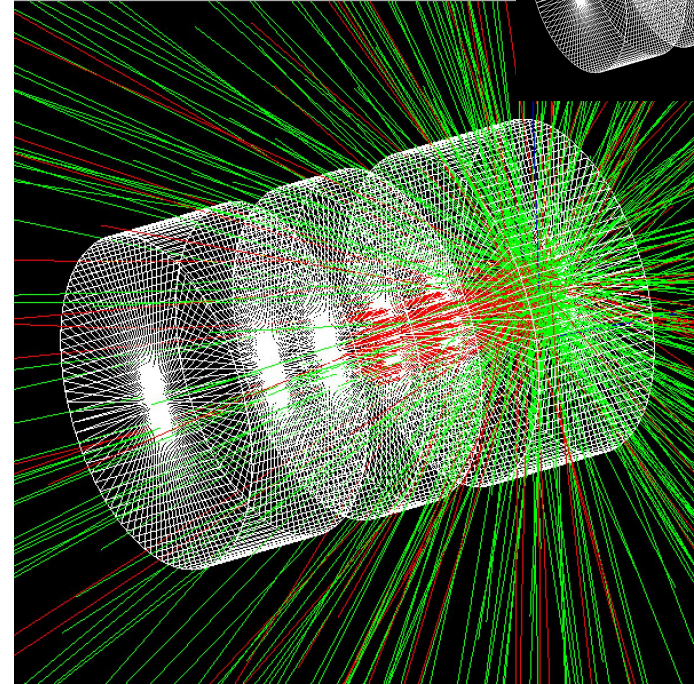


GEANT4 simulation geometries

Simulation Geometry

- Simplified geometry
 - 2.5 mm diameter diamond, 0.5 mm thick
 - High pressure DT gas cell target at 3 LHD
- 500 muons - 4.1 MeV which are slowed down to **0.7 MeV** at diamond anvil cell entry

→ **Geant4 is not useful for visualization but incredibly useful for dynamics statistics**



Muon

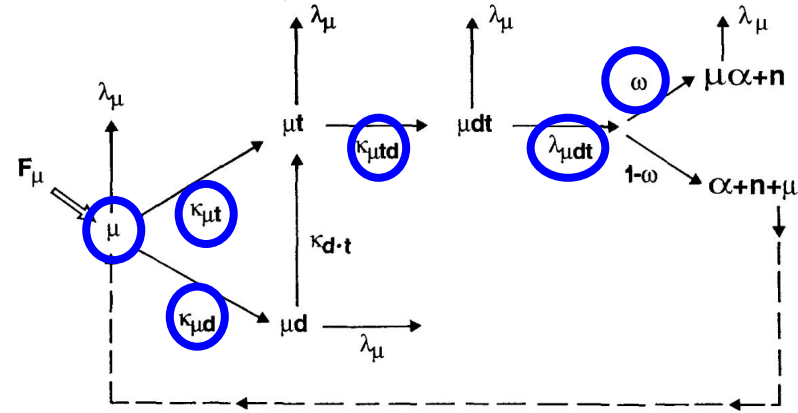
Neutron

Constant Parameters

Harms, Table 12.1

Process	Parameter	Value
Muon decay	λ_μ	$0.45 \times 10^6 \text{ s}^{-1}$
μ -d-t fusion	$\lambda_{\mu dt}$	$1.1 \times 10^{12} \text{ s}^{-1}$
Muonic atom formation	$\kappa_{\mu d}$	$1.2 \times 10^{-12} \text{ cm}^3 \text{ s}^{-1}$
Muonic atom formation	$\kappa_{\mu t}$	$1.2 \times 10^{-12} \text{ cm}^3 \text{ s}^{-1}$
Muonic molecule formation	$\kappa_{\mu dt}$	$0.25 \times 10^{-14} \text{ cm}^3 \text{ s}^{-1}$
Isotope exchange process	κ_{d-t}	$0.5 \times 10^{-14} \text{ cm}^3 \text{ s}^{-1}$
Muon sticking probability	ω	0.007

Harms, Figure 12.4



Reactivation probability = 0.30

Nuclear capture rate: $3.0 \times 10^{-4} / \text{ns}$

Alpha Sticking: $dt\mu \rightarrow \alpha\mu + n + 14.1 \text{ MeV}$

No Alpha Sticking: $dt\mu \rightarrow \alpha + \mu + n + 14.1 \text{ MeV}$

Four Experiments

1. **Initial Muon Energy:** 0.3-0.8 MeV

→ Muon stopping time + location

2. **Temperature:** 7, 10, 100-1700 K

→ Number of reactions

3. **Pressure:** 1-10 GPa

→ Number of fusion reaction per stopped muon

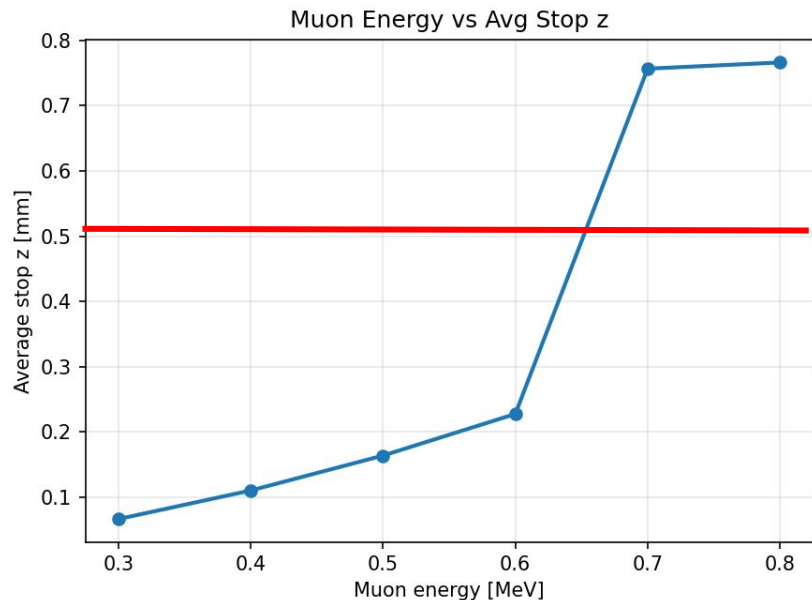
4. **T:D ratio:** 0.1-0.9

→ Energy generated

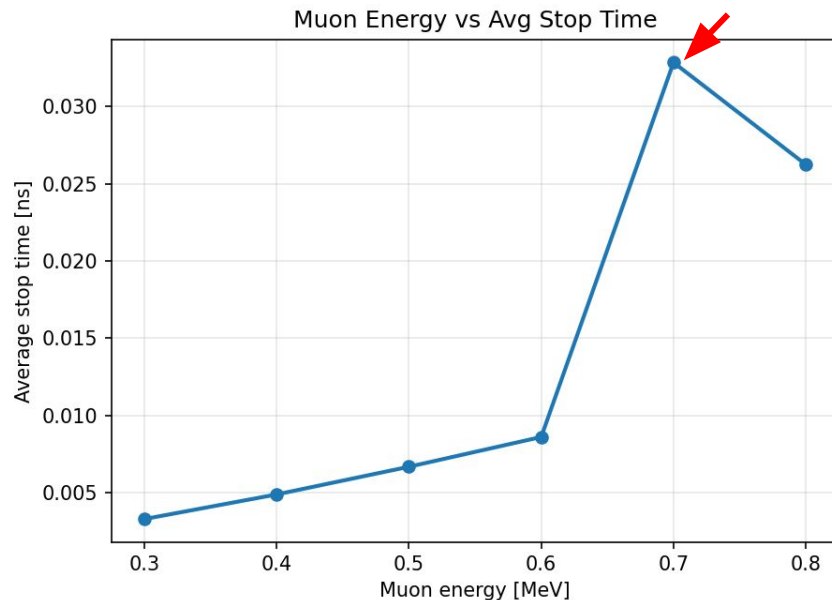
→ Muonic molecule formation rate (rate limiting step)

→ Neutron flux

Initial Muon Energy \rightarrow Muon Stopping Location + Time

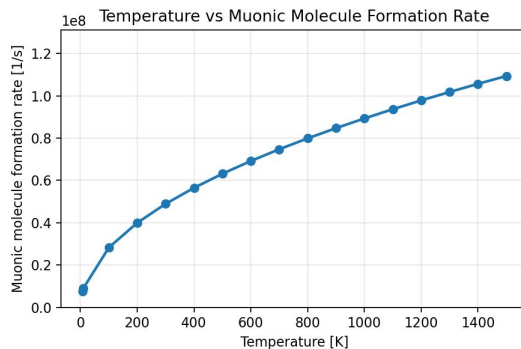
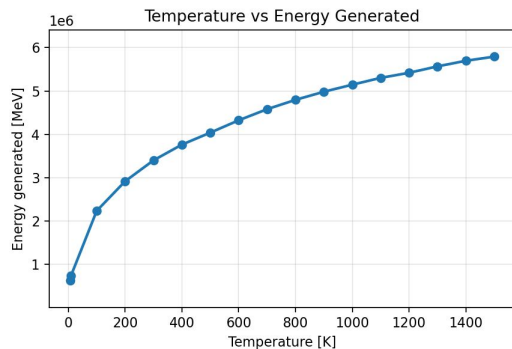
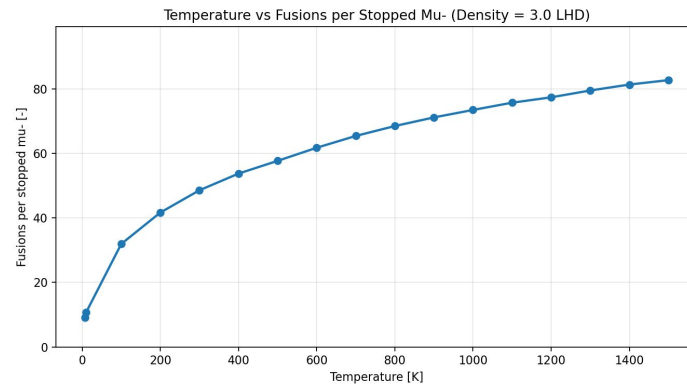
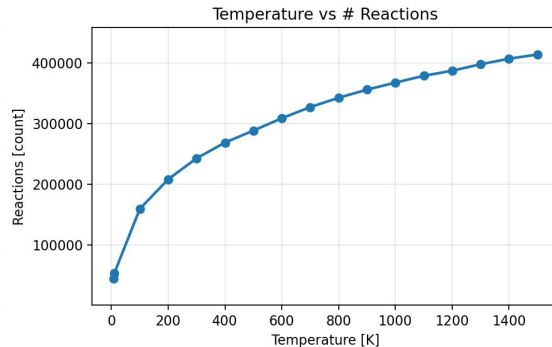
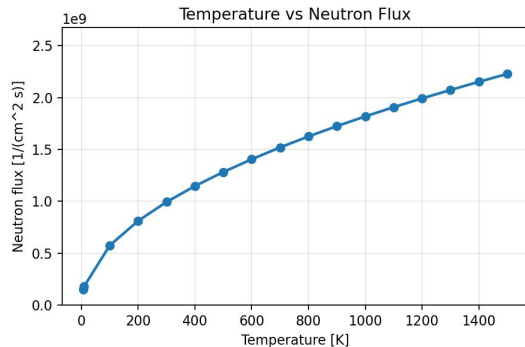



\rightarrow need muon to enter diamond at ~ 0.7 MeV



\rightarrow takes around 0.03 ns for muon to reach target from diamond anvil cell entry
 \rightarrow sudden decrease due to muon slamming into back of diamond anvil cell

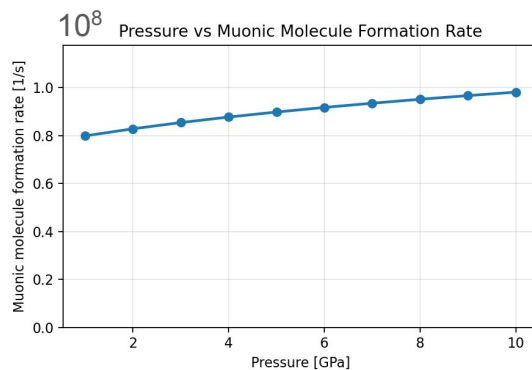
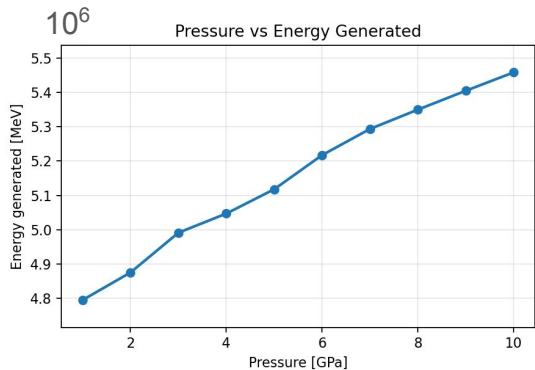
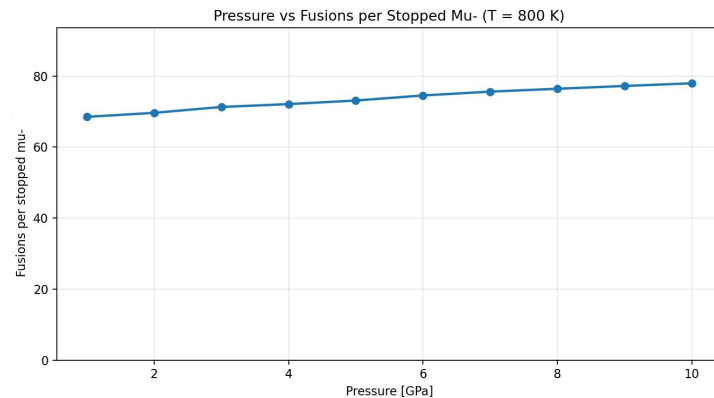
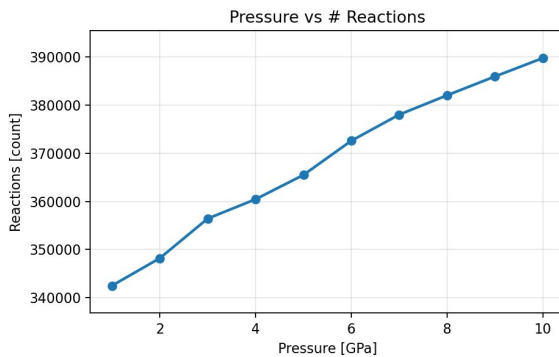
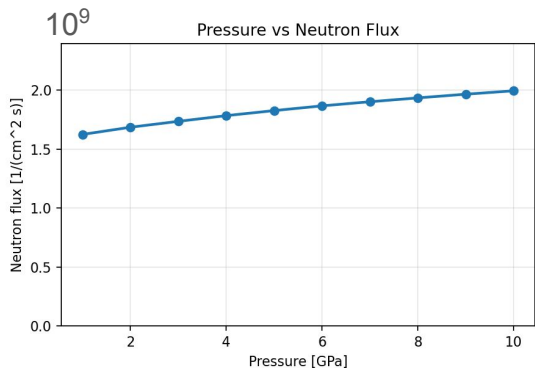
Temperature $P = 5 \text{ GPa}$



$T \uparrow$ 

- \uparrow # reactions
- \uparrow energy produced
- \uparrow neutron flux
- \uparrow muonic molecule formation rate

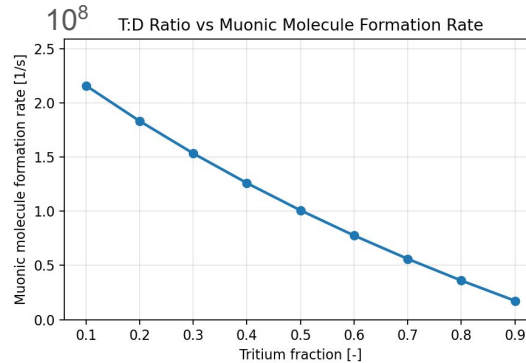
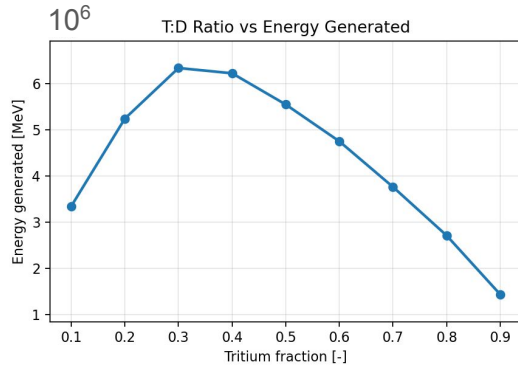
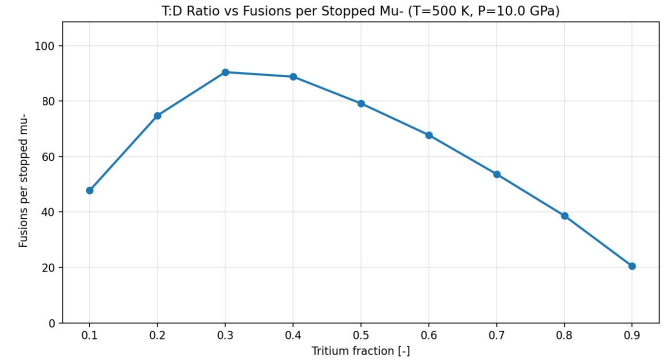
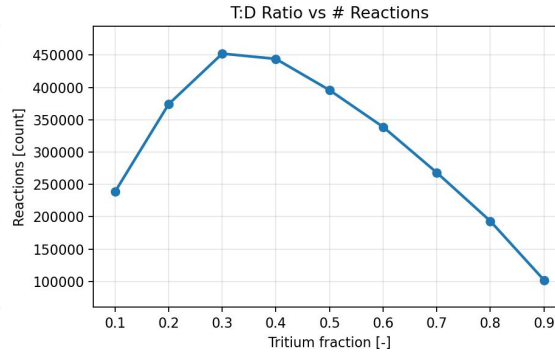
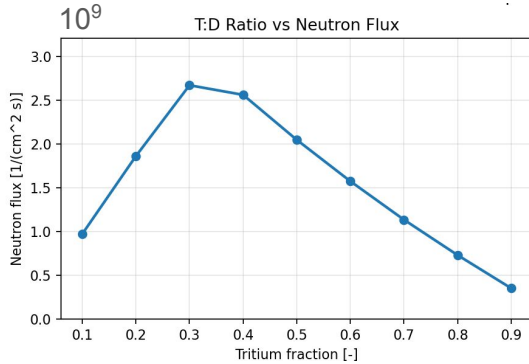
Pressure $T = 800$ K



P ↑ →

- ↑ # reactions
- ↑ energy produced
- ↑ neutron flux
- ↑ muonic molecule formation rate

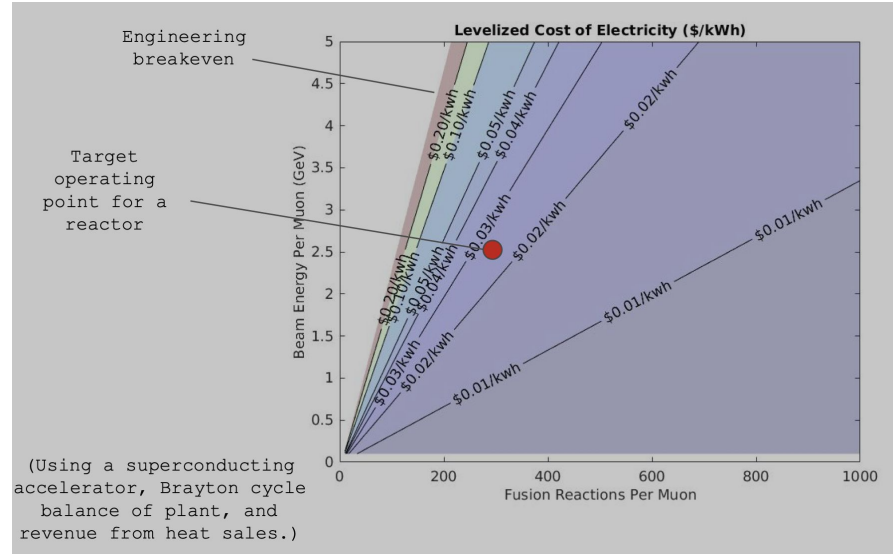
T:D Ratio $T = 500 \text{ K}, P = 10 \text{ GPa}$



- 30% T:D best for # reactions and energy generated
- Acceleron: 35% Tritium used
- Muonic molecule formation rate compromised slightly and neutron flux high (as has been with greater number of reactions)

Takeaways for MCF Dynamics

- Ideal temp: 500-800K
- Ideal pressure: as high as possible, without causing diamond cracking (10 GPa)
 - 10 GPa, 800K, 30% T:D ratio
- Initial muon energy (at least 0.7 MeV)
- 300 reactions/muon is the goal - must solve alpha sticking and reactivation issue

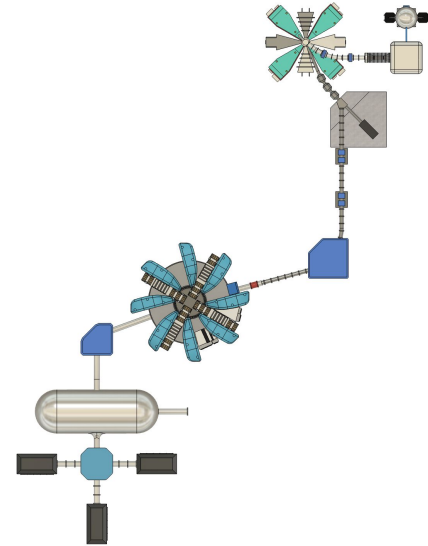


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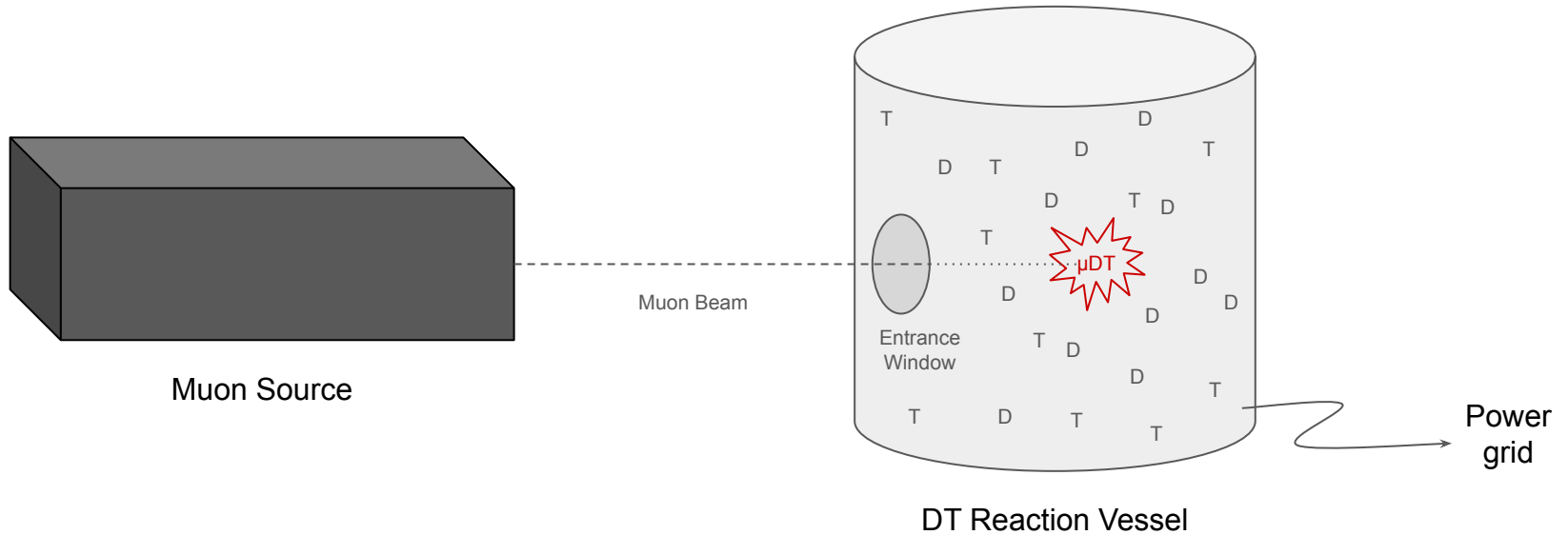
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- [6] NASA, “Title of Report,” NASA Technical Reports Server (2008), available at <https://ntrs.nasa.gov/api/citations/20080040752/downloads/20080040752.pdf>.
- [7] Geant4 Collaboration, “Geant4 Source Code: Hadronic Stopping Processes,” GitHub repository (accessed 2026), <https://github.com/Geant4/geant4/tree/b4a16de652ec244f7a0ecc0a5cacfee21930bf75/source/processes/hadronic/stopping/include>.

2. Designing a Muon Source in CAD - Thomas

- a. Review of muon sources/muon generation
- b. Overview of CAD
- c. Pre-Accelerator
- d. Injector
- e. Transfer Optics
- f. Primary Accelerator
- g. Target



What's a Muon Source?

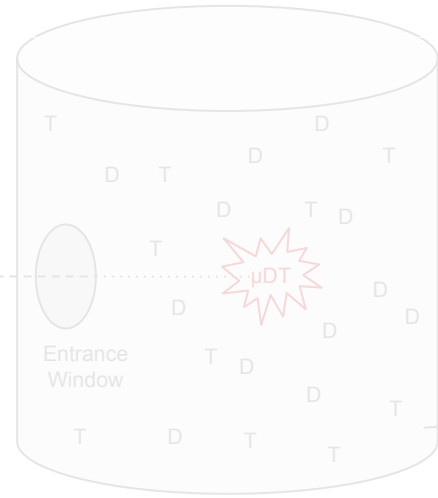


What's a Muon Source?



Muon Source

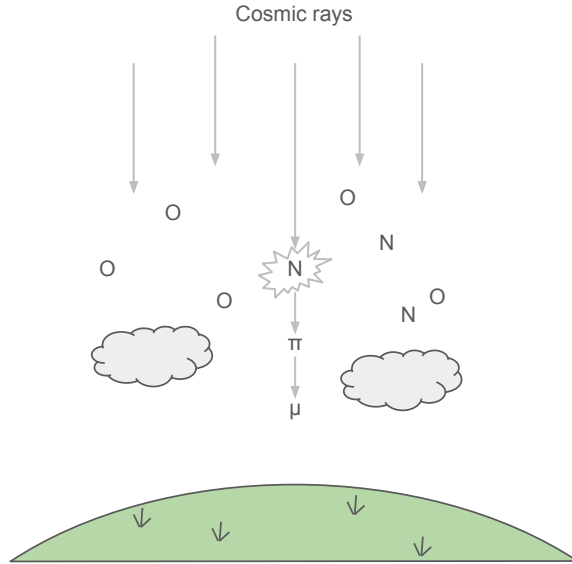
Muon Beam



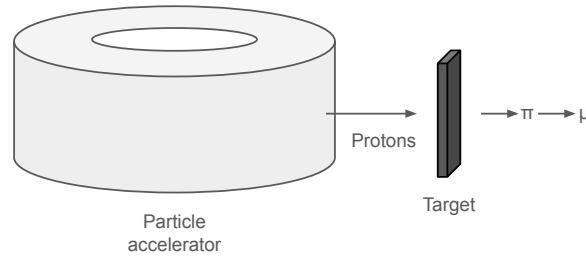
DT Reaction Vessel

Power grid

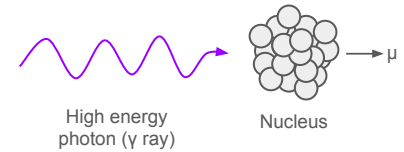
Ways to generate muons



Cosmic Ray Spallation

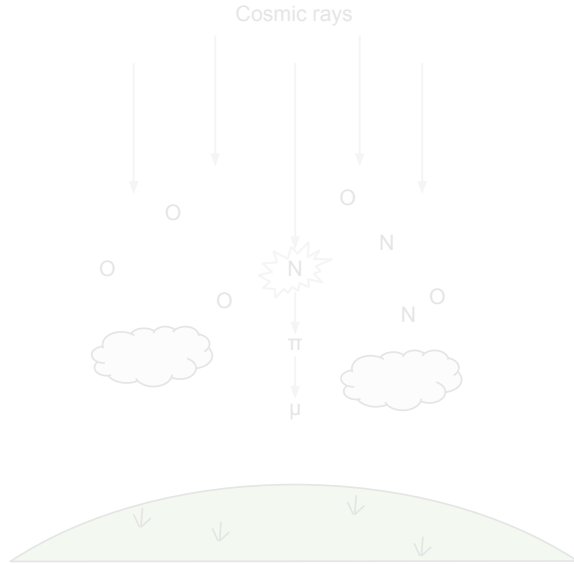


Particle Accelerators

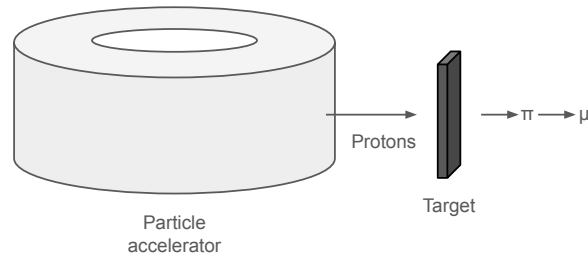


Photoproduction

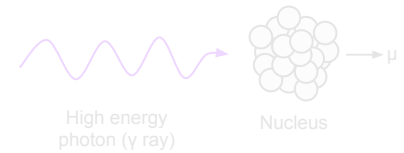
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Cosmic Ray Spallation




Particle Accelerators

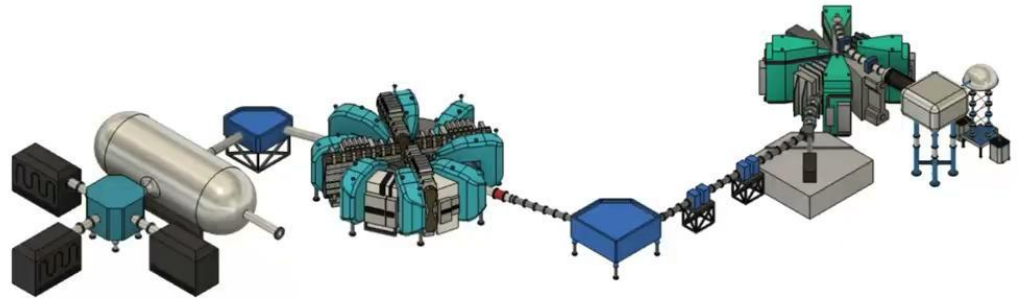


Photoproduction

My Proposed Muon Source



Amalgamation of existing muon facility designs and research papers

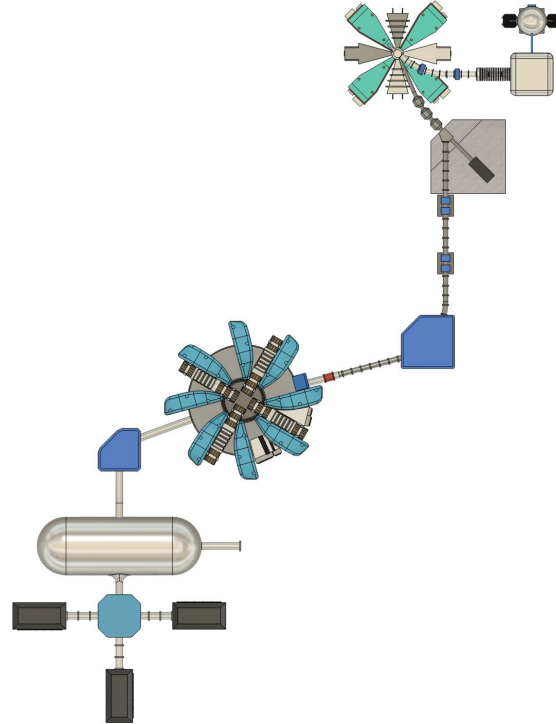
-  **PSI (primary)**
-  **TRIUMF**
-  **ISIS**



My Proposed Muon Source

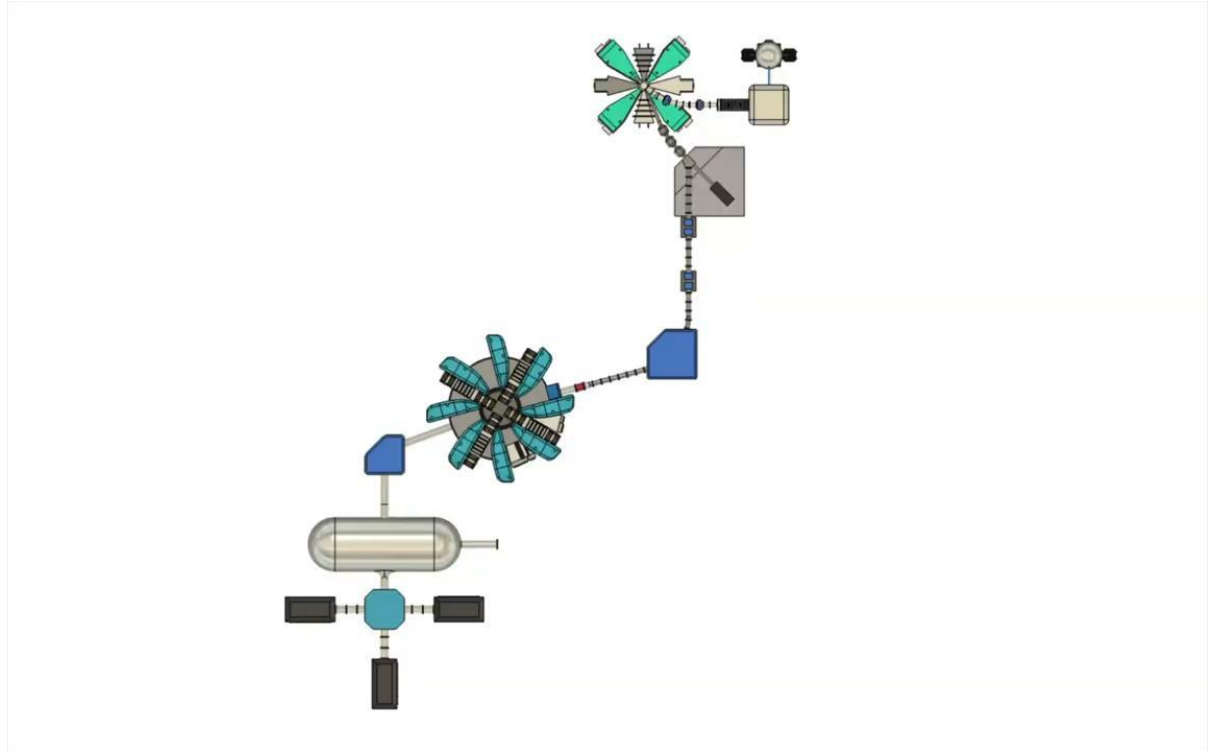
Amalgamation of existing muon facility designs and research papers

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Pre-Accelerator

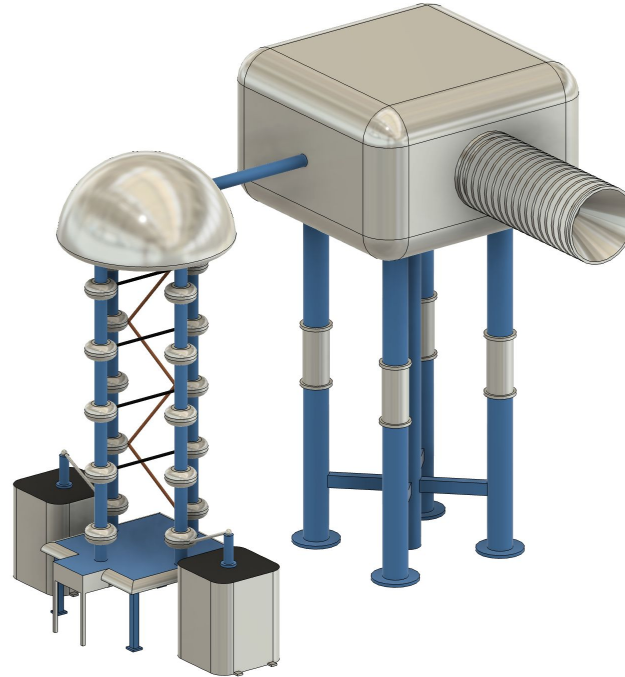
- Preconditions protons for initial cyclotron (injector)
- Cockcroft-walton (CW) architecture
 - Diode/capacitor tower recitifes low-voltage AC → high-voltage DC
 - 810 kV (4% speed of light)
- Proton source
 - 1100 W, 2.45 GHz microwave H gas cavity
 - 10-12 mA (~10 trillion protons)
- Acceleration
 - 60 keV (source) + 810 keV (acceleration) = 870 keV output



Pre-accelerator > Injector > Transfer optics >
Primary Accelerator > Target

Pre-Accelerator

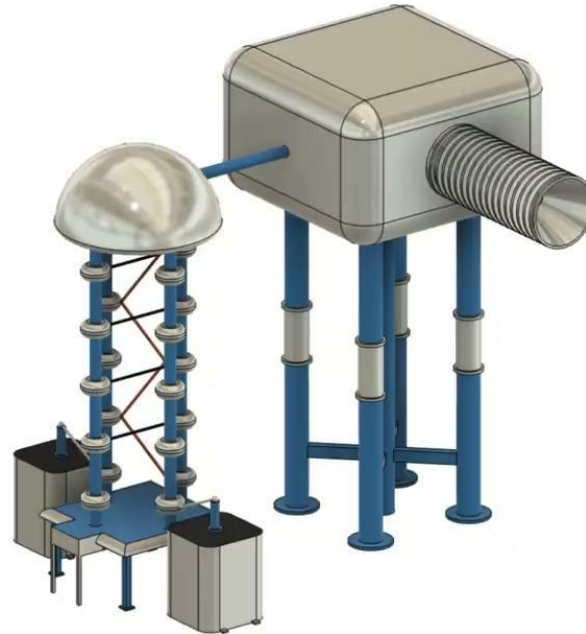
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Injector

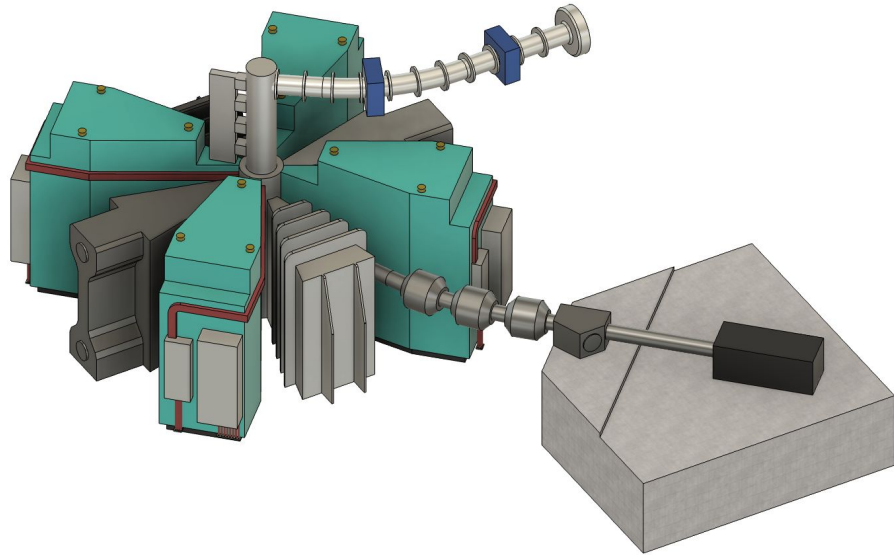
- Preconditions protons for primary cyclotron
- Separated sector cyclotron
 - 4 magnets
 - 2 RF resonators (50 MHz)
 - 2 secondary RF resonators (150 MHz)
- 72 MeV output (38% speed of light)
- 2.2 to 2.4 mA output beam current
- Acceleration routine
 - Injected in middle via 2x 90° turns
 - 80 orbits inside
 - Electrostatic extraction



Pre-accelerator > **Injector** > Transfer optics >
Primary Accelerator > Target

Injector

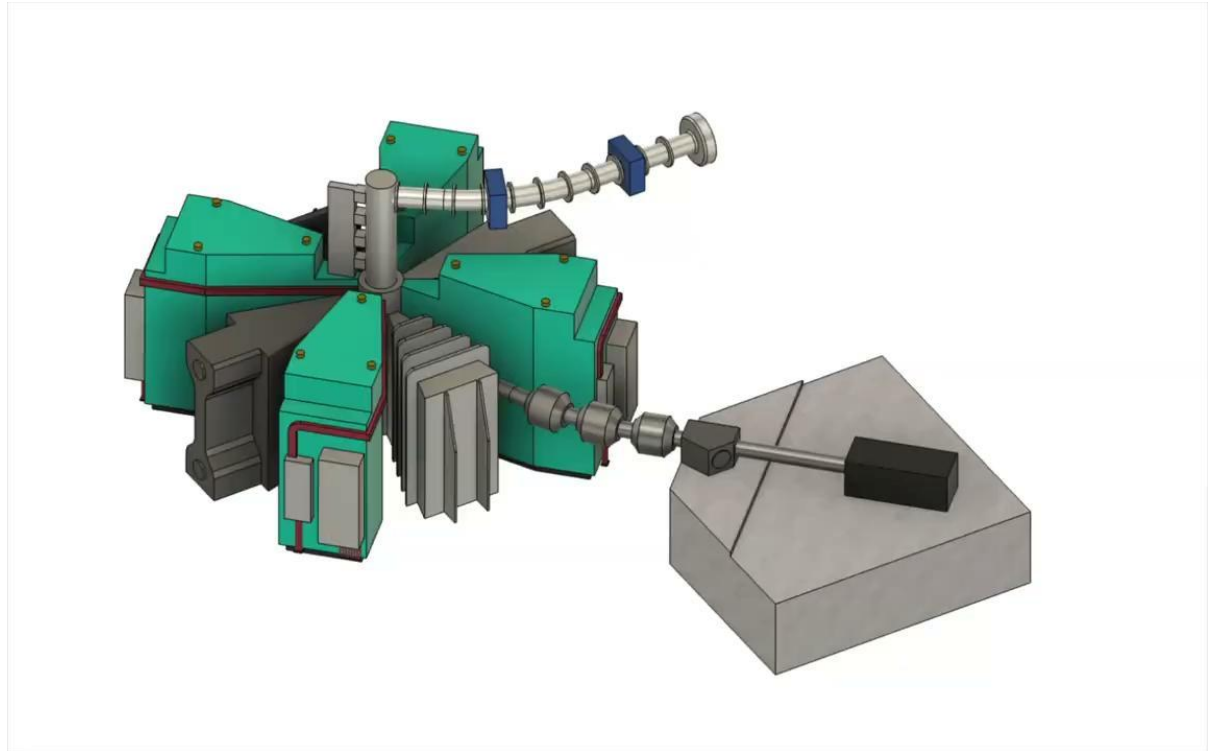
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Pre-accelerator > **Injector** > Transfer optics >
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Transfer Optics

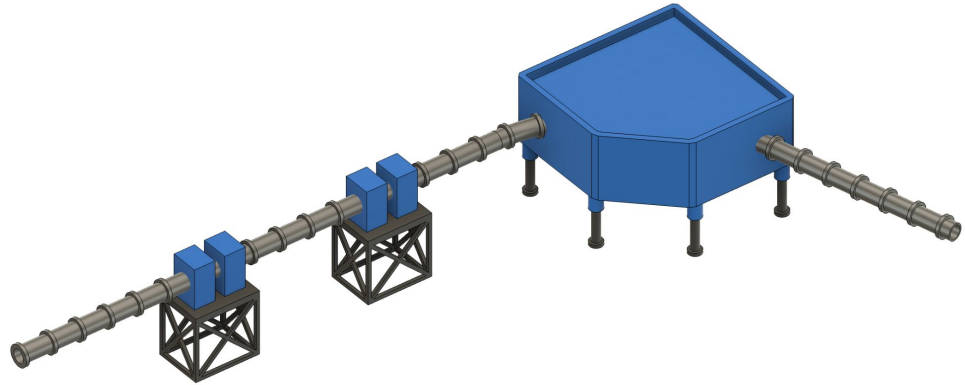
- Transports protons from injector to primary accelerator
- Evacuated stainless steel tube
- Dipole magnets used for steering in corners
- Quadrupole magnets squeeze beam
 - Always come in pairs (horizontal & vertical compression)
- Beam dump shielded block of metal
 - Used for startup and emergency stop
 - ~10 ms to 100 ms to melt through stainless steel
 - Emergency system detects fault in 100 μ s



Pre-accelerator > Injector > Transfer optics >
Primary Accelerator > Target

Transfer Optics

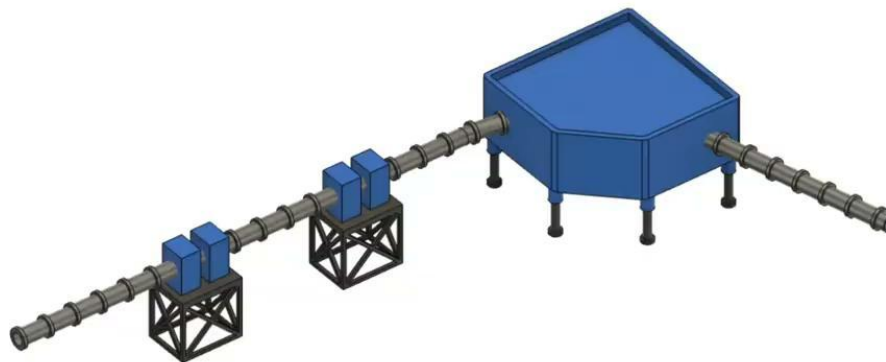
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Pre-accelerator > Injector > Transfer optics >
Primary Accelerator > Target

Primary Accelerator

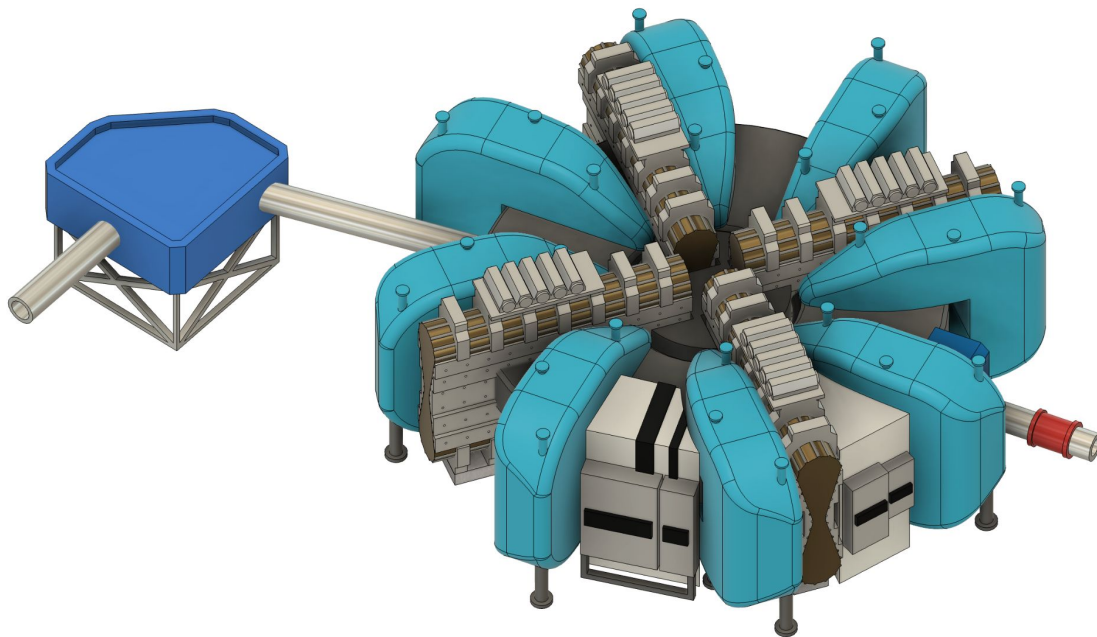
- Accelerators preconditions protons up to final KE
- Ring cyclotron
 - 8 sector magnets
 - 4 RF resonators (50 MHz)
- 15 meter outer diameter
- 186 orbits to reach extraction
- Final beam characteristics
 - 1.4 MW
 - 5 - 7 mm beam diameter
 - 2.2 mA output current
 - 590 MeV output (79% speed of light)



Pre-accelerator > Injector > Transfer optics >
Primary Accelerator > Target

Primary Accelerator

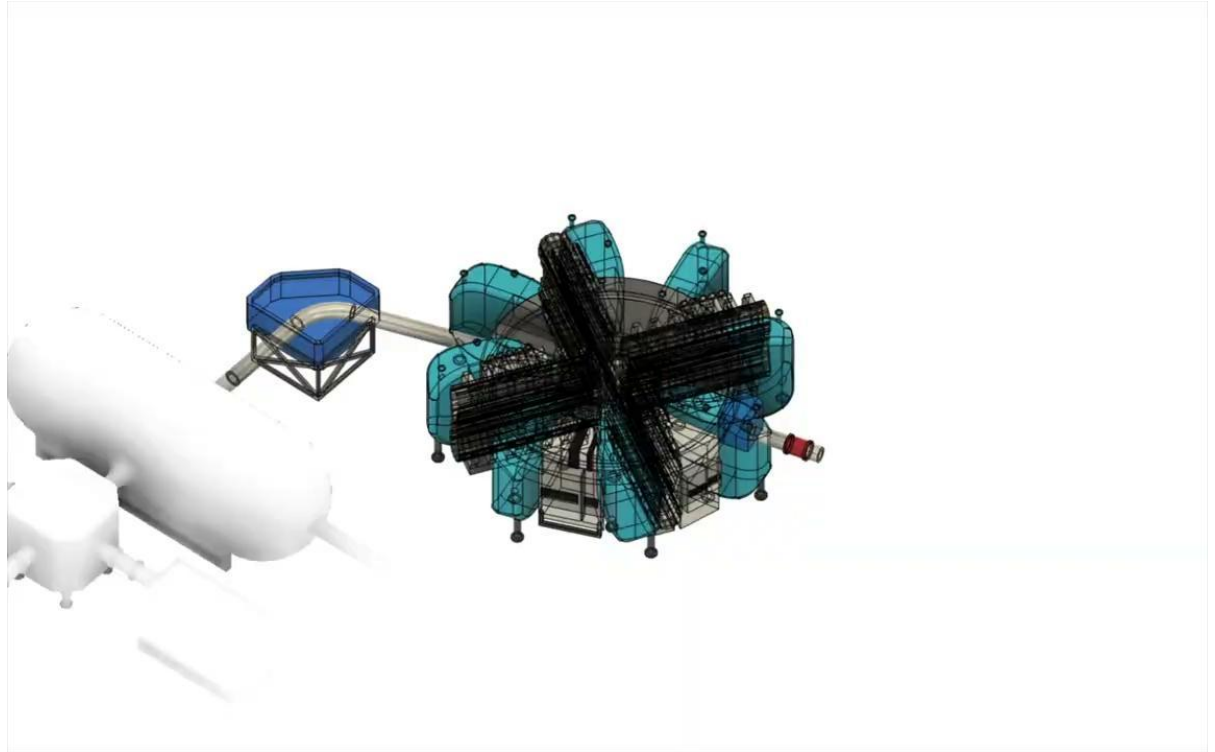
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Pre-accelerator > Injector > Transfer optics >
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Target

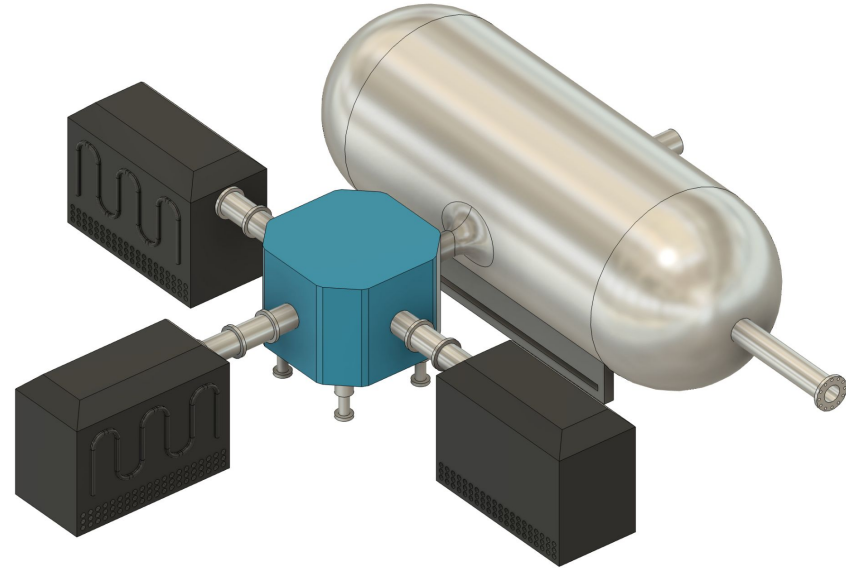
- Produces Muons from impinging protons on nuclei
- Two spinning carbon wheel targets
- Carbon (isotropic graphite)
 - Low Z avoids neutrons/Bremsstrahlung
 - High thermal conductivity & sublimation temp
- 5 cm thick
 - Minimizes internal pion absorption
 - Minimizes total heat flux
- Beam dump
 - Proton beam split between 3 metal beam dumps
 - Cooling recovers heat



Pre-accelerator > Injector > Transfer optics >
Primary Accelerator > Target

Target

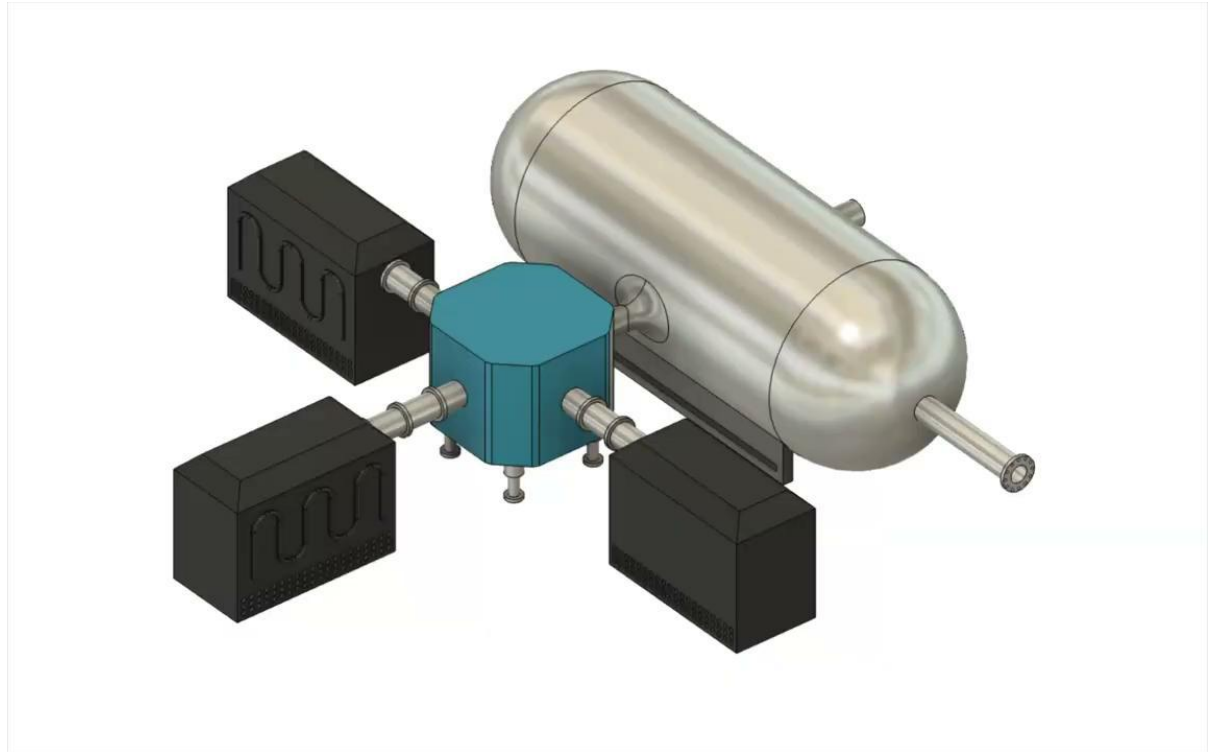
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Pre-accelerator > Injector > Transfer optics >
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Summary

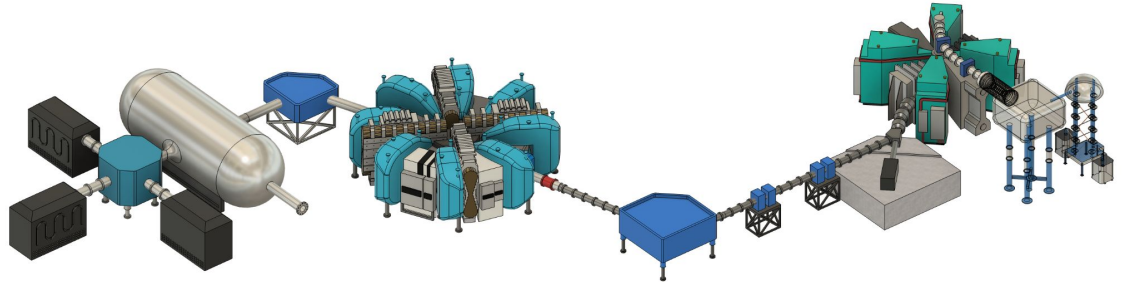
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- Injector further accelerates protons to 72 MeV, injects into primary accelerator
- Cyclotron accelerates protons to final energy of 590 MeV
- Protons smashed into target producing pions, which decay into muons



Pre-accelerator > Injector > Transfer optics >
Primary Accelerator > Target

Summary

- Cockcroft-Walton pre-accelerator generates protons, gets them to ~810 keV
- Injector further accelerates protons to 72 MeV, injects into primary accelerator
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Pre-accelerator > Injector > Transfer optics >
Primary Accelerator > Target

Sources

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Thank you!

Supporting Slides

Thomas

Layout of PSI

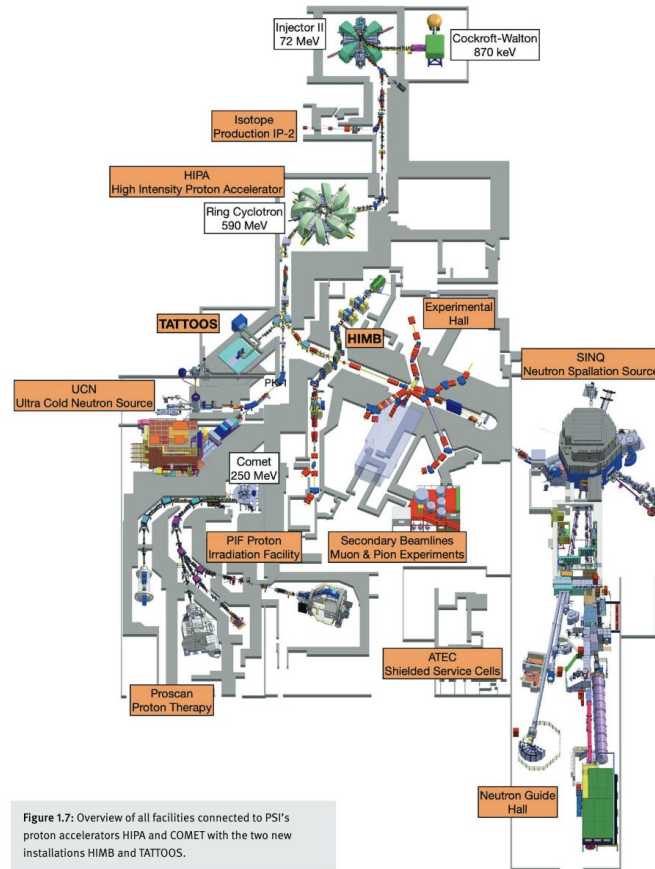
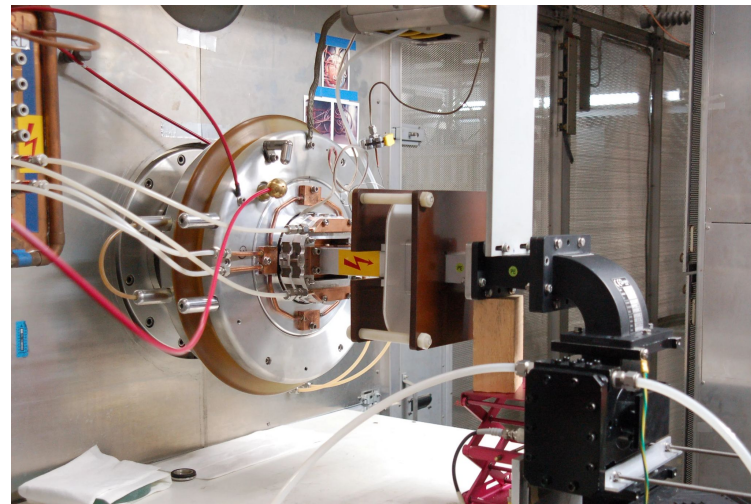
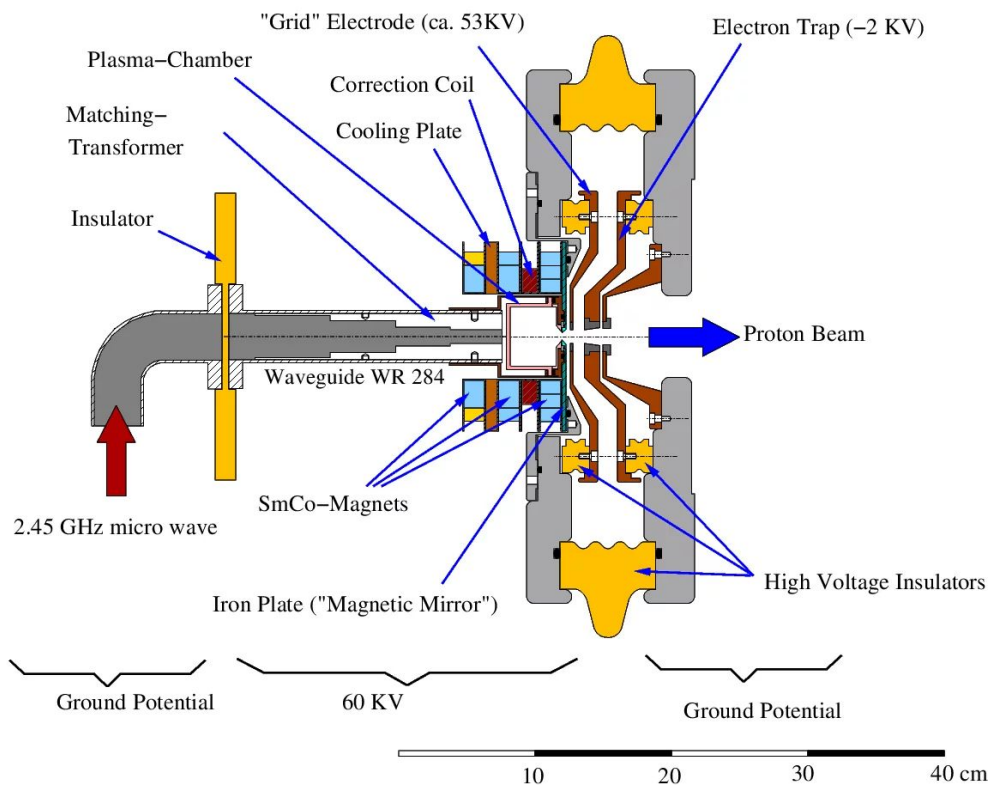
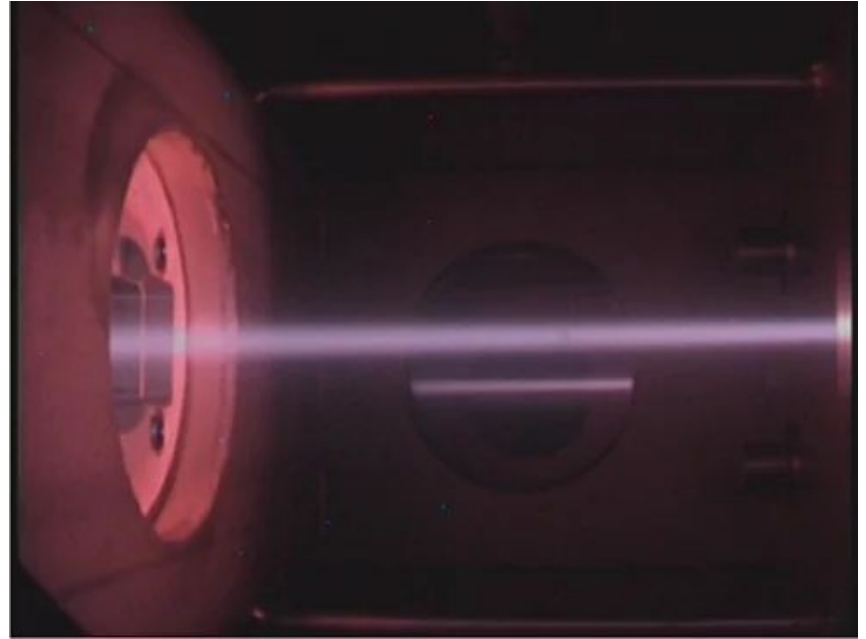
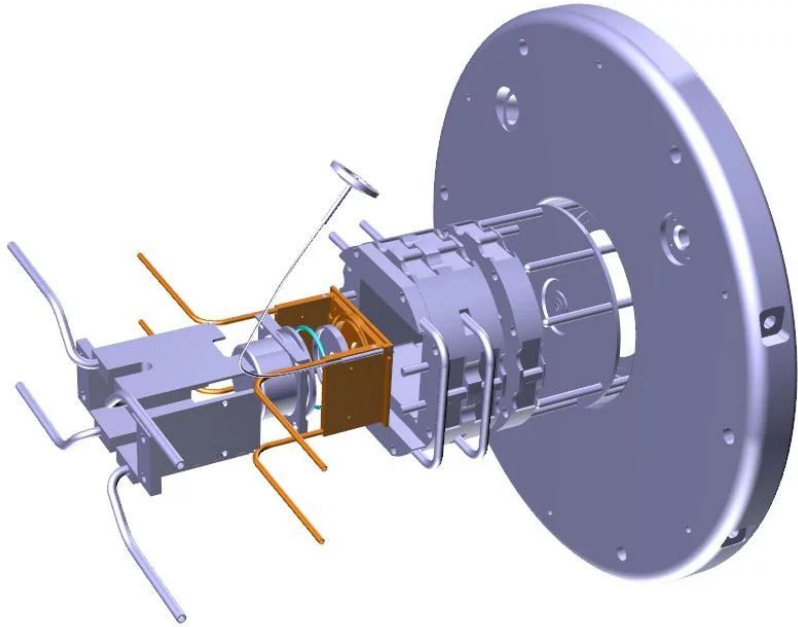


Figure 1.7: Overview of all facilities connected to PSI's proton accelerators HIPA and COMET with the two new installations HIMB and TATTOOS.

H⁺ Source (PSI) (Slide 1/2)



H⁺ Source (PSI) (Slide 2/2)



Proposed High Pressure DT Cells

Figure 6.7: μ SR uniaxial pressure cell available currently at PSI.
From [Hicks, 2017].

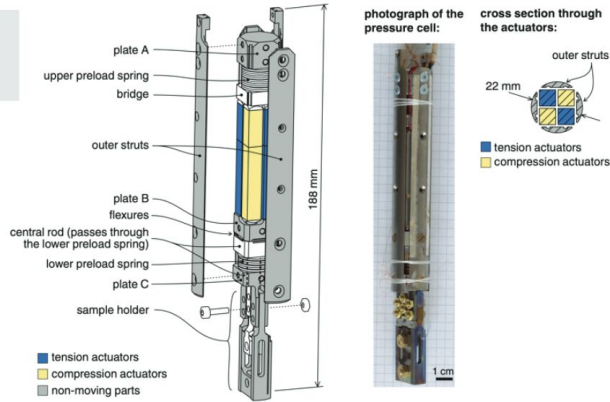


Figure 6.6: (a) Cross-sectional view of the PSI double wall piston-cylinder pressure cell for μ SR; (b) Details of the pressure seal.
From [Khasanov, 2016].

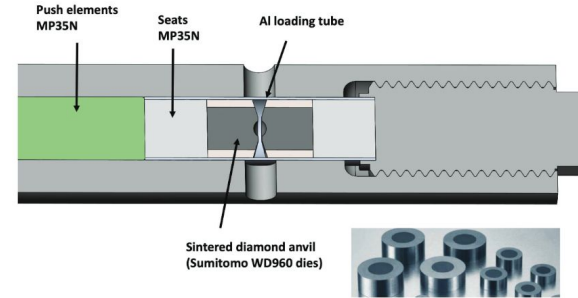
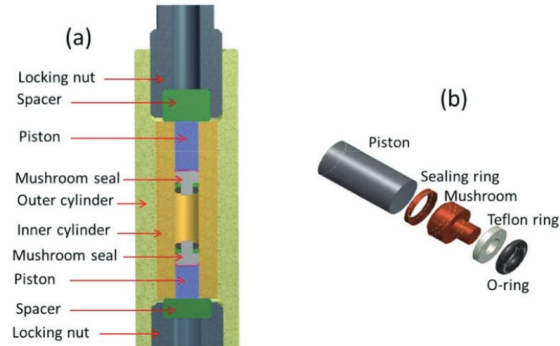


Figure 6.8: Concept of novel μ SR high-pressure anvil cell currently under development within the SNF R'Equip project ExtremeP.

Radial Beam Intensity of Primary Accelerator

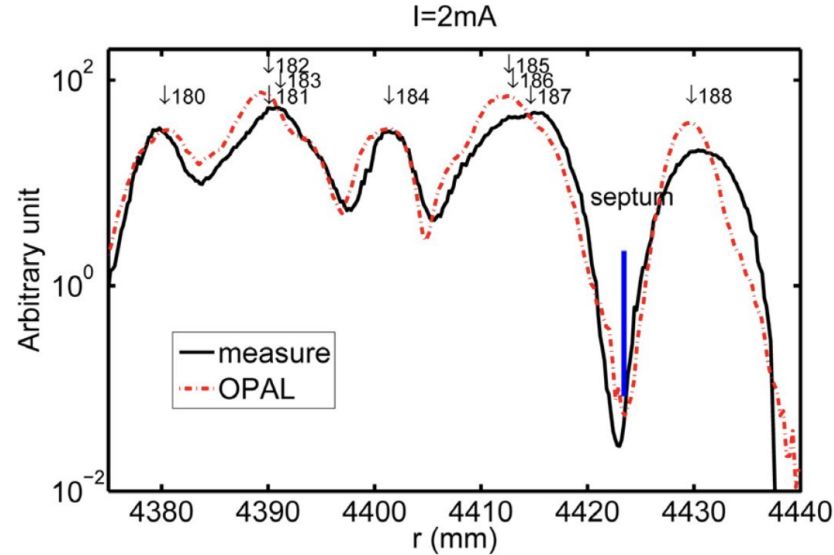
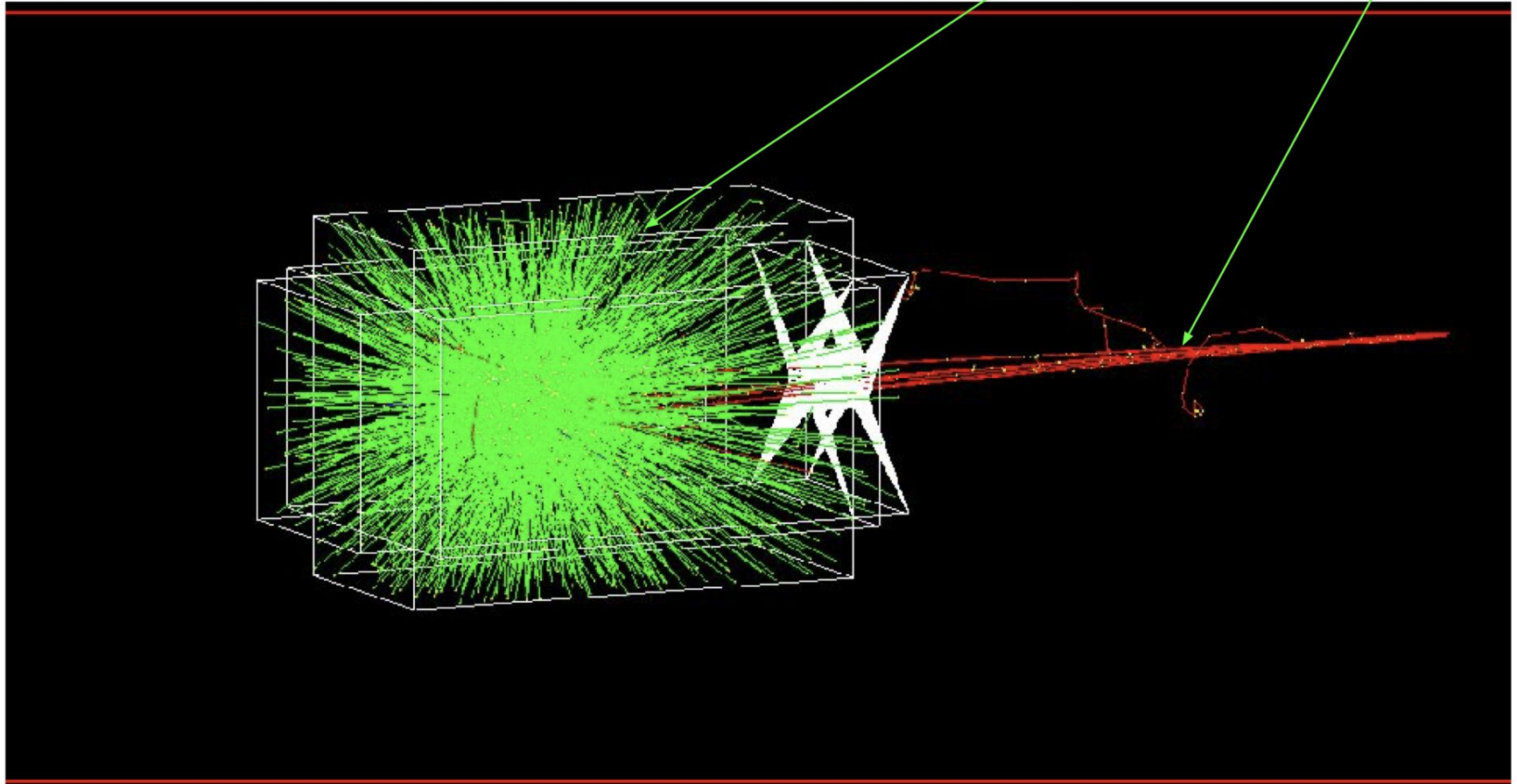
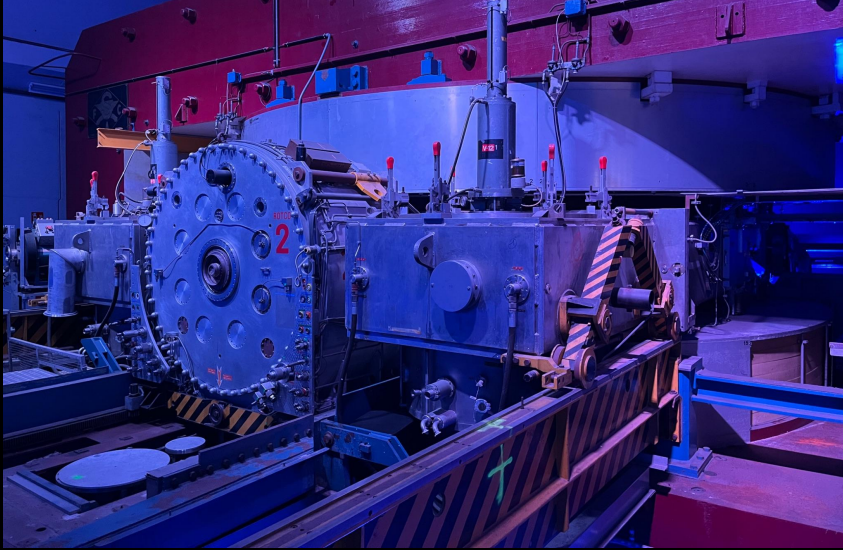


Figure 3: Radial beam profile with indicated turn numbers at extraction. The density is minimized at the location of the extraction electrode.

Himani



Synchrocyclotron



Antimatter Factory

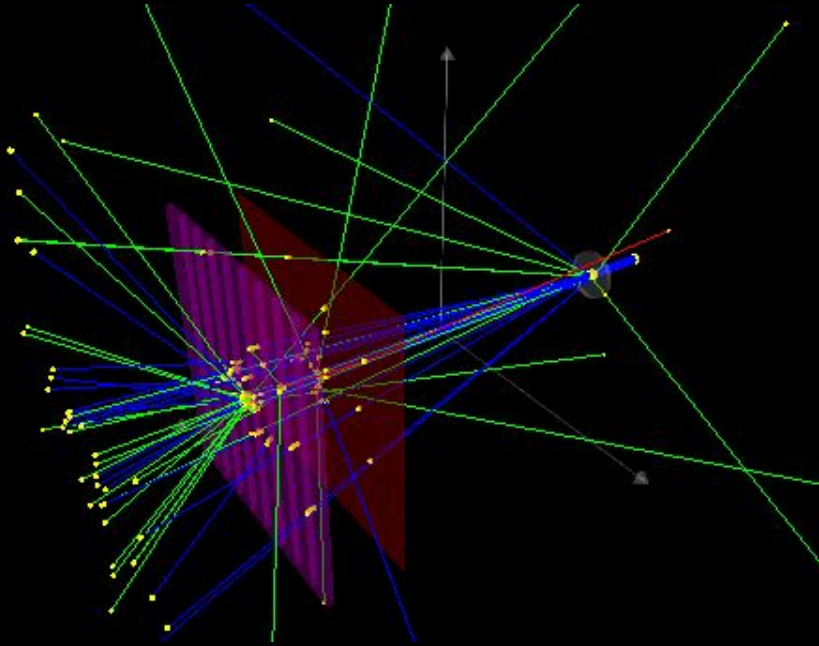


ATLAS Control Room

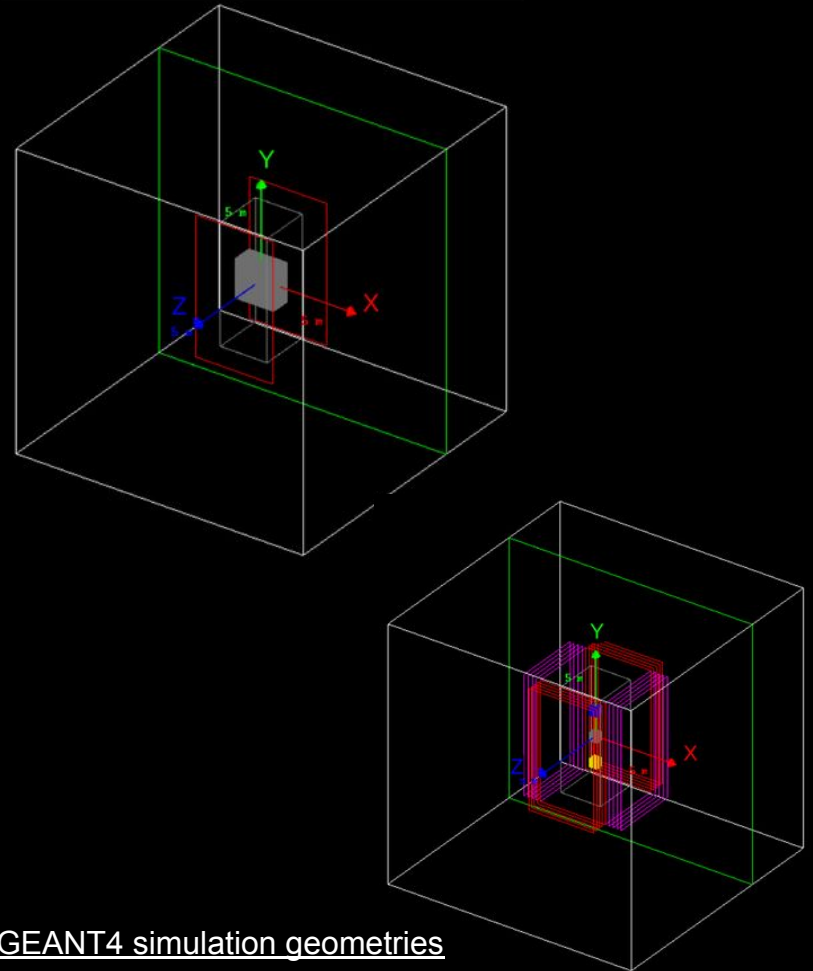


CERN Experiments Using Geant4

Geant4



a GEANT4 Simulation | Nuclear Physics 101



GEANT4 simulation geometries